

3D-PTV and Lagrangian measurements in a wind tunnel

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NCTR, April 7-12, 2019

Outline

- What is the three-dimensional particle tracking velocimetry
- What is the main contribution to turbulence research
- What are the limitations and possible solutions
- The (only) working solution example - Ron Shnapp

The take-home message

- You can do it and you better do it
- Real-time image analysis on a dedicated hardware is a key for long-recording, high-speed 3D-PTV
- Paradigms about 3D-PTV changes from in-lab table-top experiments to wind tunnel and field experiments
- You can readily get data sets of millions of tracer trajectories like the one recorded in a canopy flow model in an environmental wind tunnel, providing Lagrangian velocity and acceleration distributions in an urban canopy flow model

Details are in the pre-print “Real-time extension ...” by Shnapp et al. [arXiv:1806.04975](https://arxiv.org/abs/1806.04975)

Let's follow the Lagrangian path



“Marianthe” invited people inside turbulent forms to experience them as if they were a particle borne along in the flow. Athena Tacha (1985), “Nautilus” by Philip Ball

Basic steps

Image acquisition by a multi camera arrangement



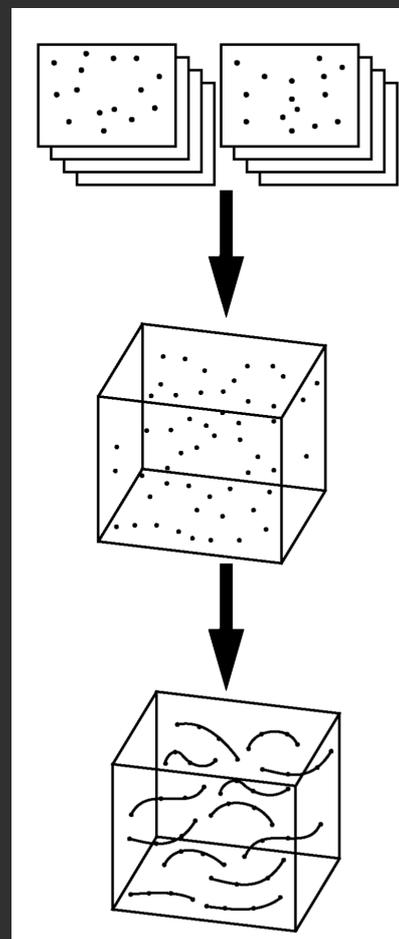
Particle detection



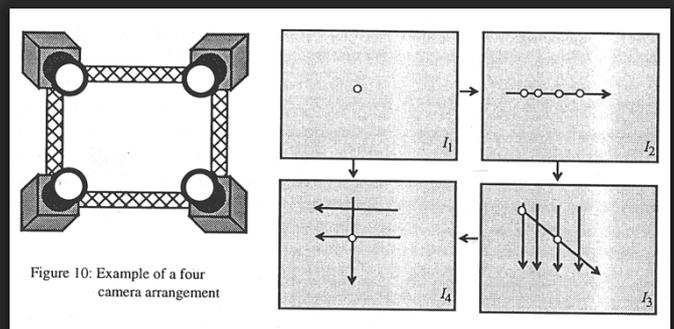
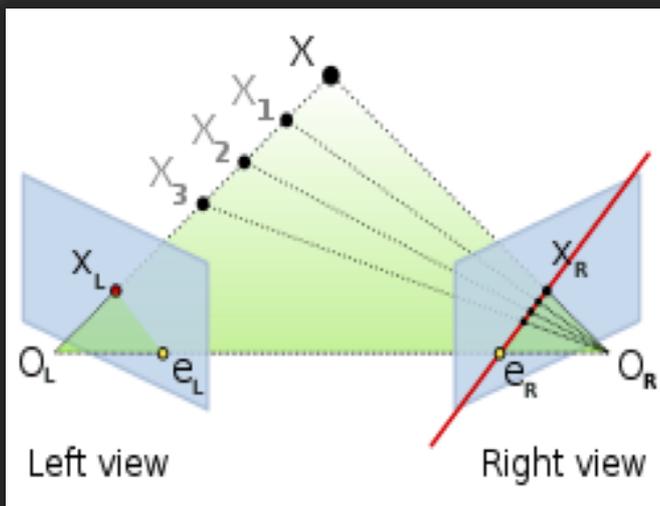
Establishment of stereoscopic correspondence



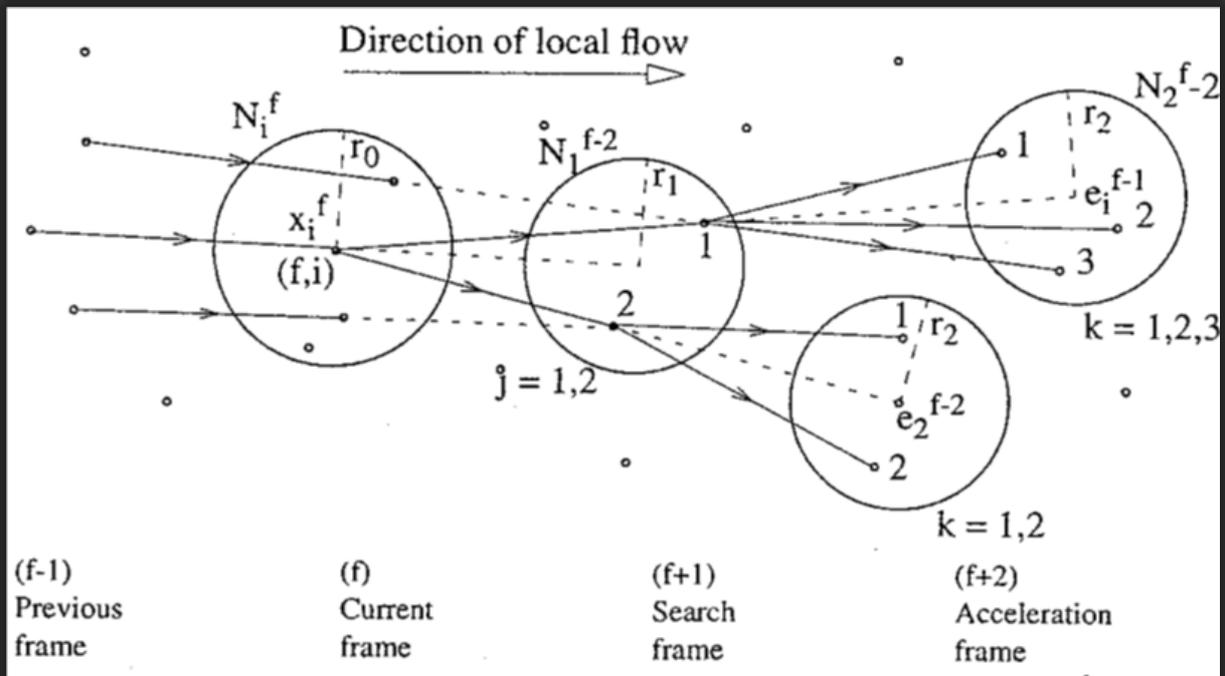
Particle tracking in 3D space



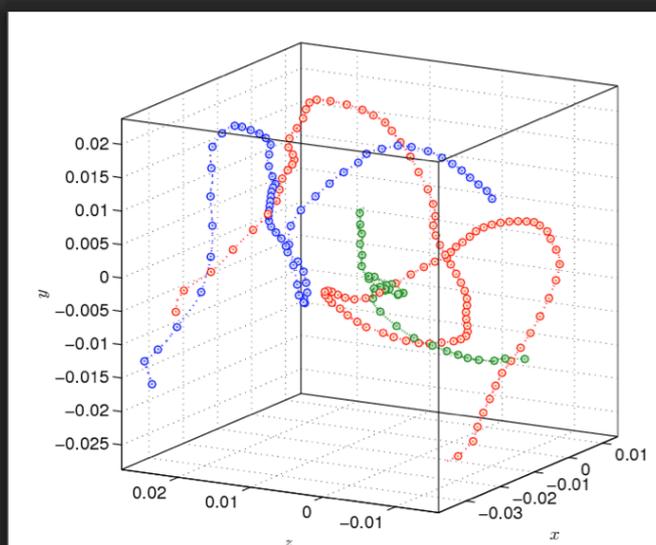
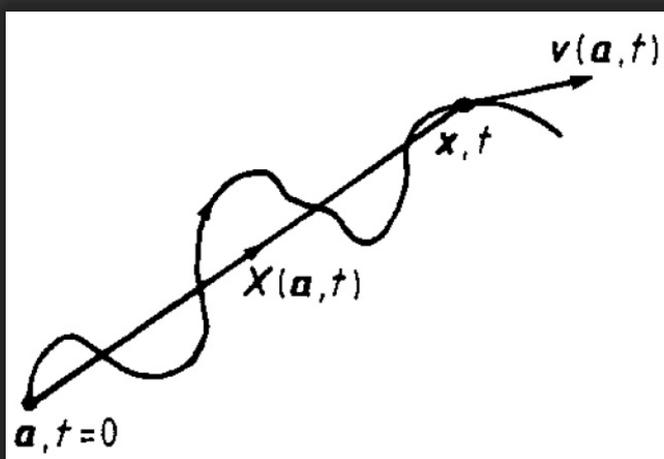
Epipolar geometry



Tracking

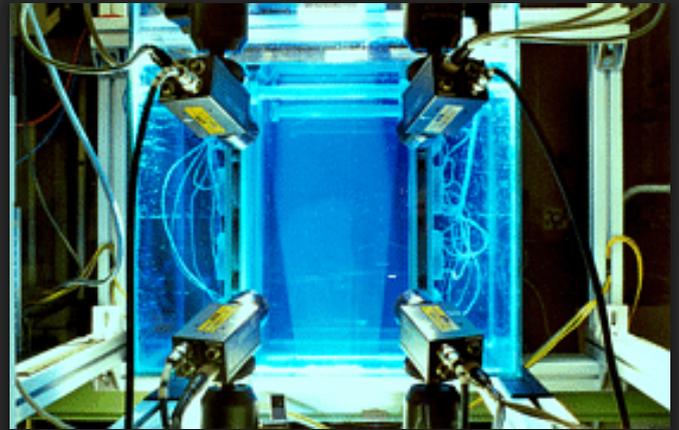
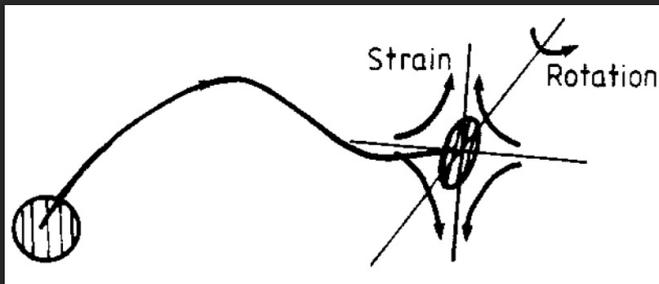


The immediate result is a Lagrangian trajectory

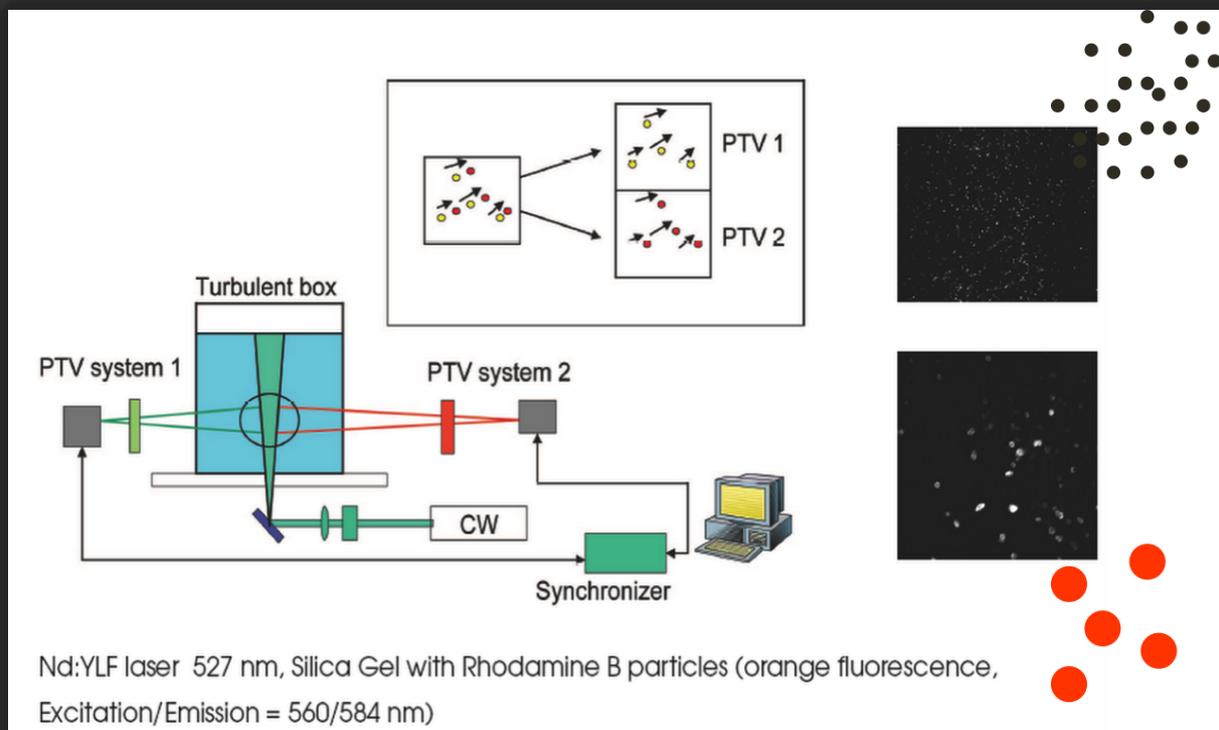


3D-PTV main focus is turbulence

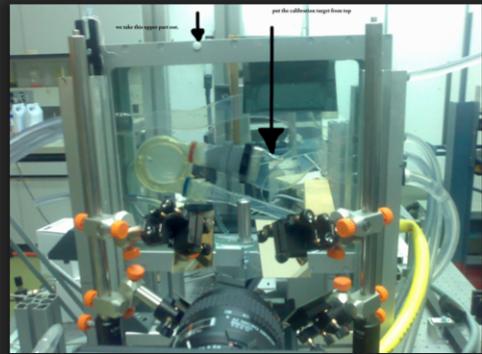
Which means we need the **full gradient tensor** along the particle trajectories: $\partial u_i / \partial x_j$ in space and time



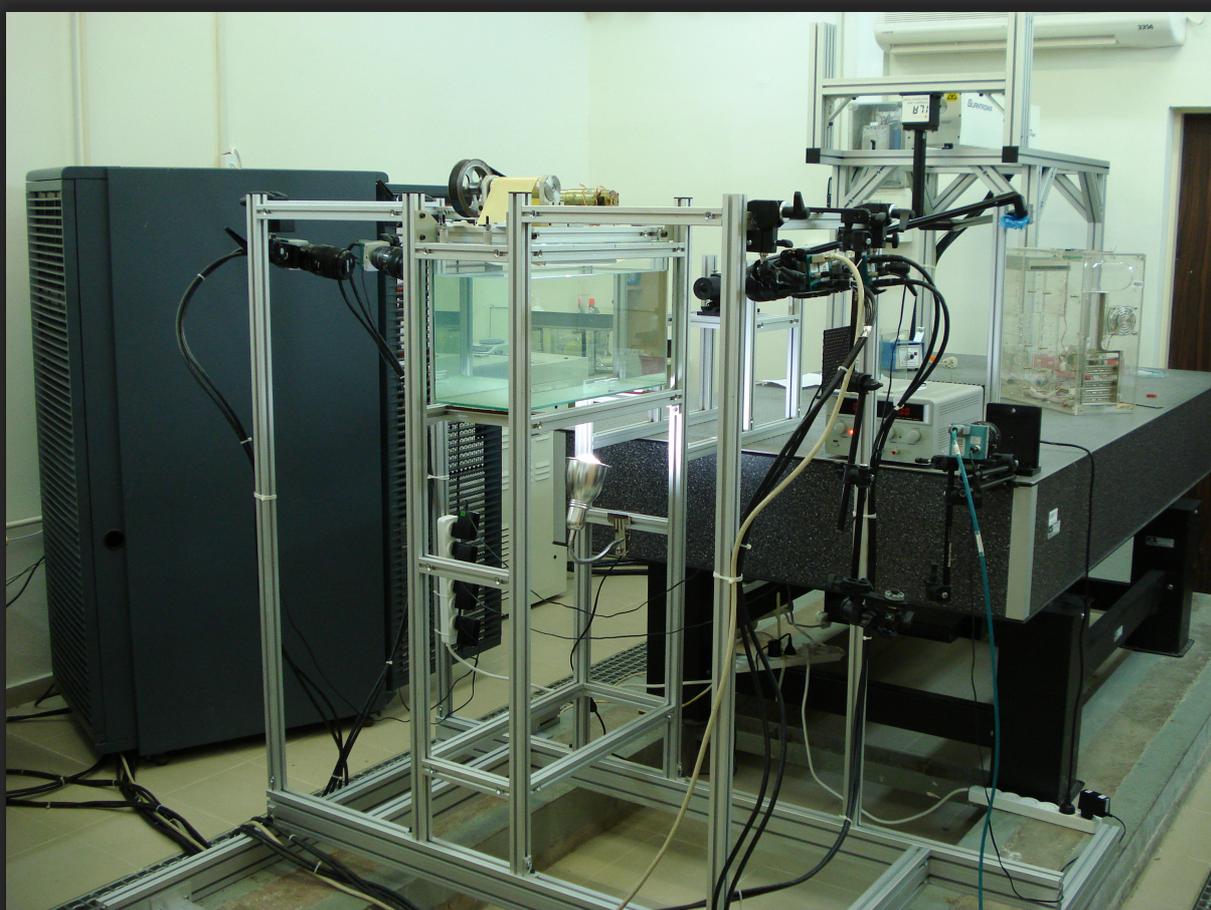
It had other applications, e.g. inertial clustering



MRI + 3D-PTV



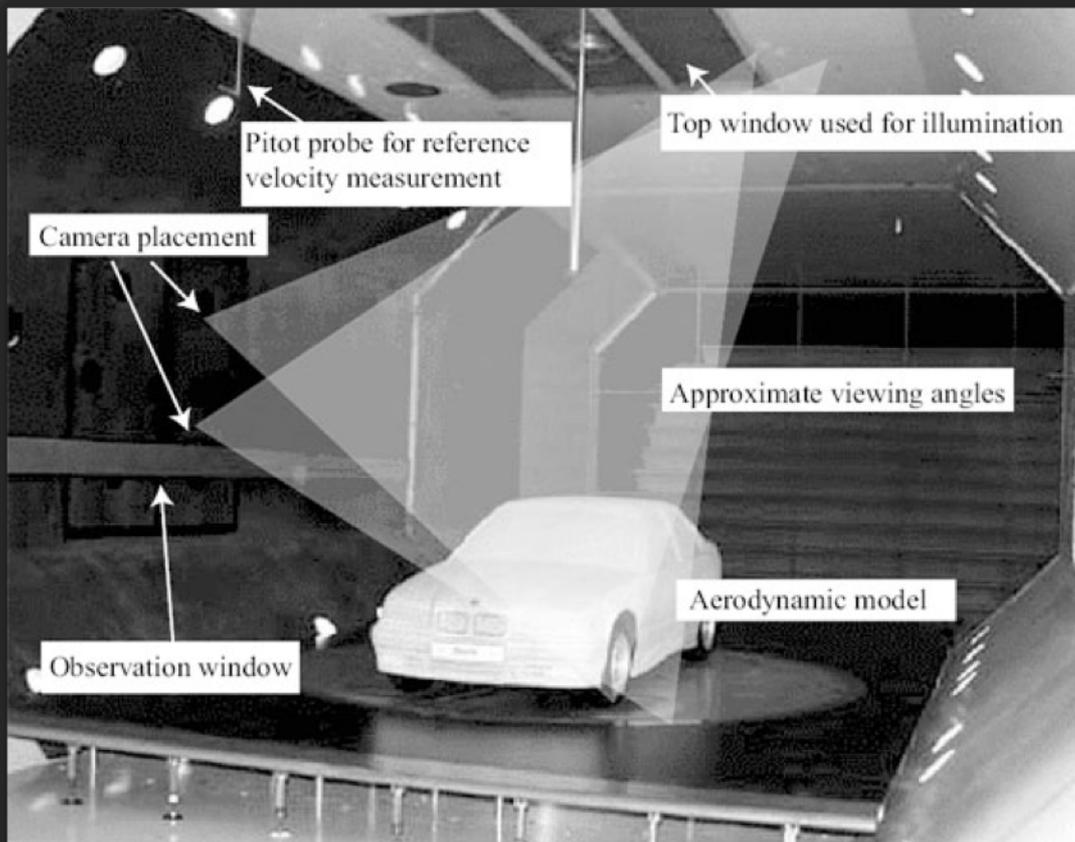
3D PTV is typically a lab system



The main bottleneck is also heavy

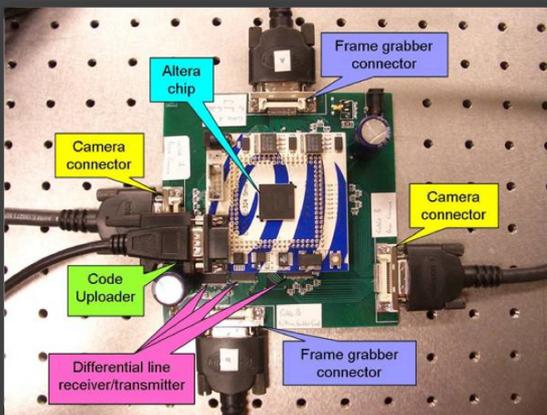
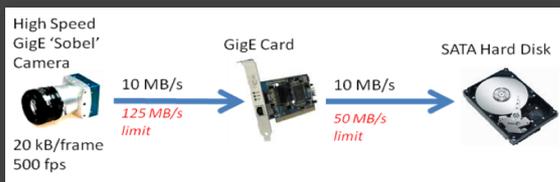


We had a dream: 3D-PTV for large scale systems

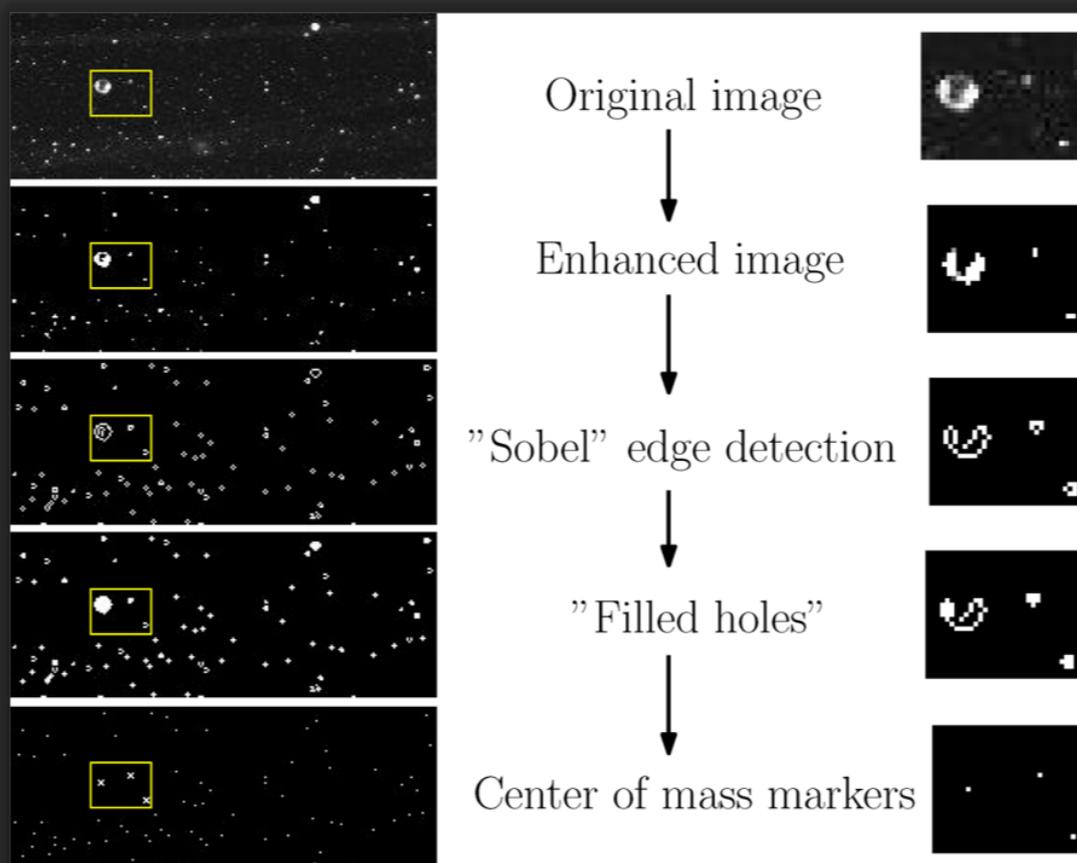


Need to eliminate the transfer rate bottleneck

from compression to on-camera processing



Sobel edge detection based algorithm

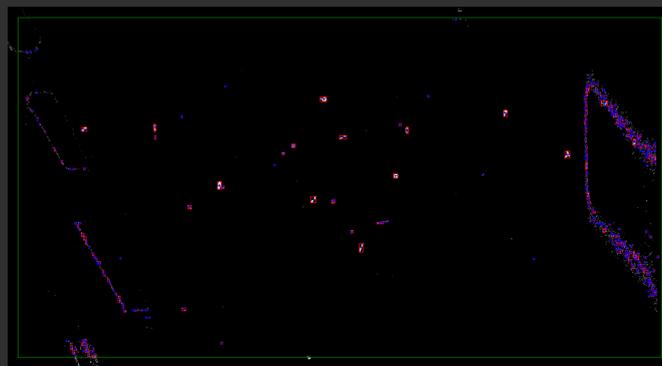
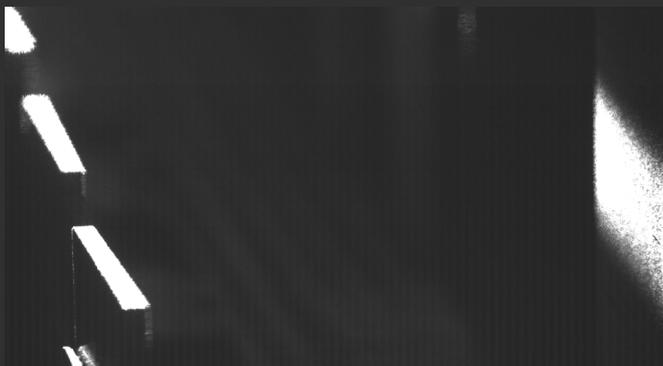


Works very well for lab experiments



Raw image - binarized image - blobs marked on the original image.

Real life is not like this



Raw 3D-PTV image the wind tunnel experiments: Background - ζ binary image after background subtraction, and detection using a local adaptive filter

We had to develop the know-how

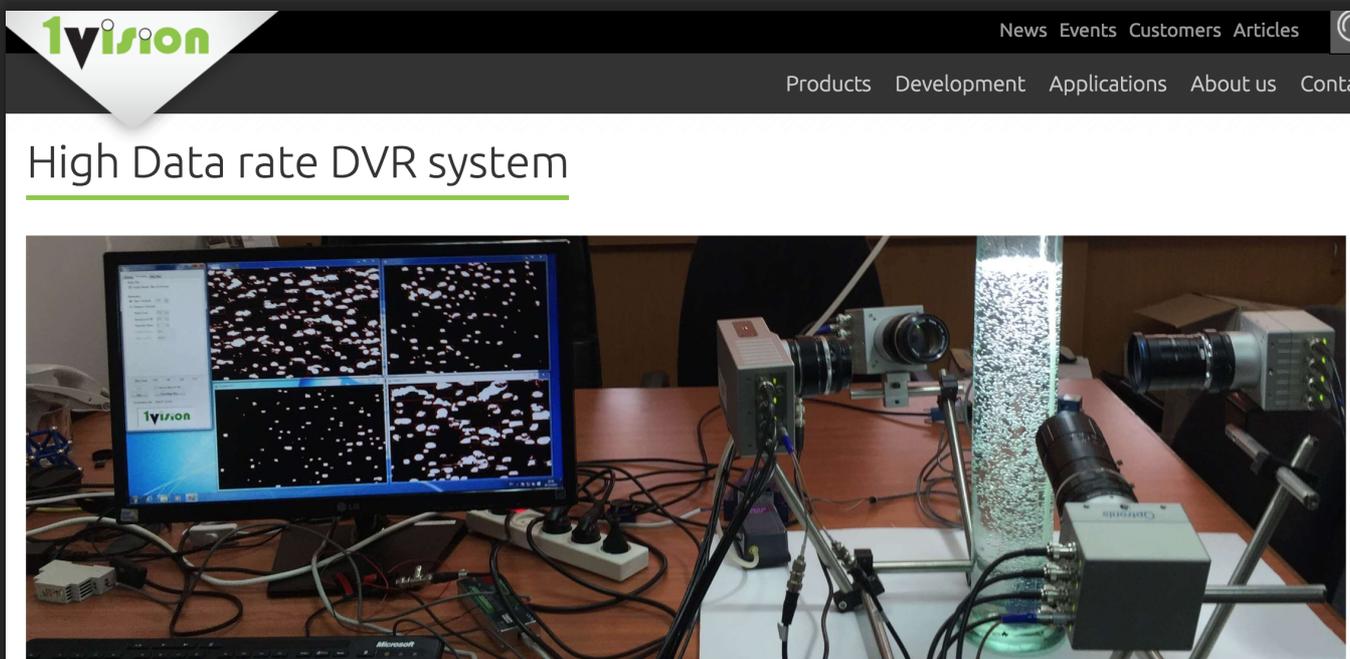
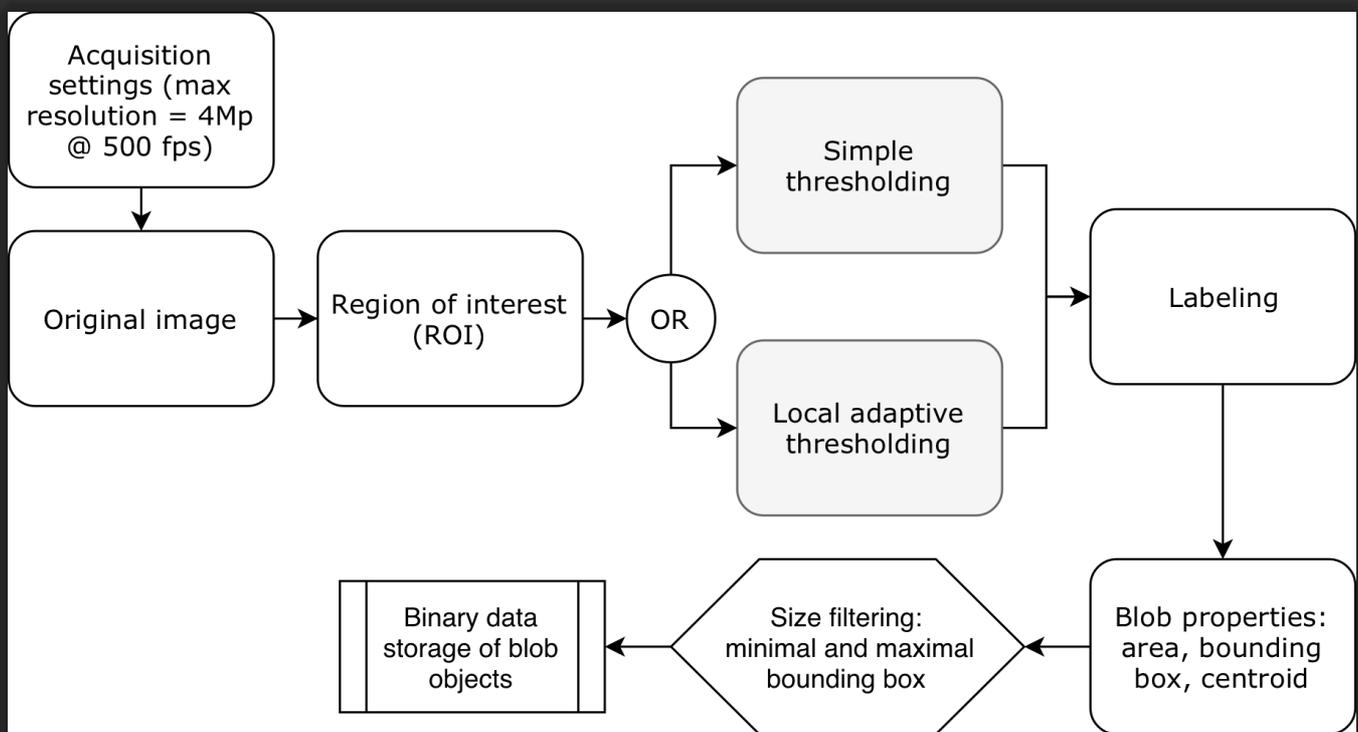


Image processing algorithm on FPGA



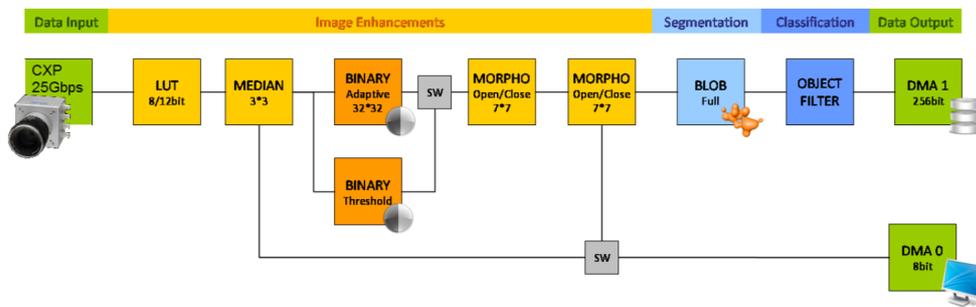
And its implementation on a dedicated hardware

Your Vision, Our Mission

Image Processing & DVR System:

4 x 4MP @ 500 fps - Total 8GB/sec Data Rate

- 4 x Optronis High-Speed Cameras: **4 MPixels @ 500 FPS**
- 4 x Silicon-Software Frame Grabbers w/**CoaXPRESS** Interface
- Real-Time **Image Processing** by FPGA on Frame Grabber board
- Software Application for **Blobs Data Recording & Display**
- OpenPTV - Application for **Particle Tracking Velocimetry**



And now we are ready for the Environmental Wind Tunnel



Open source software suite, all on Github

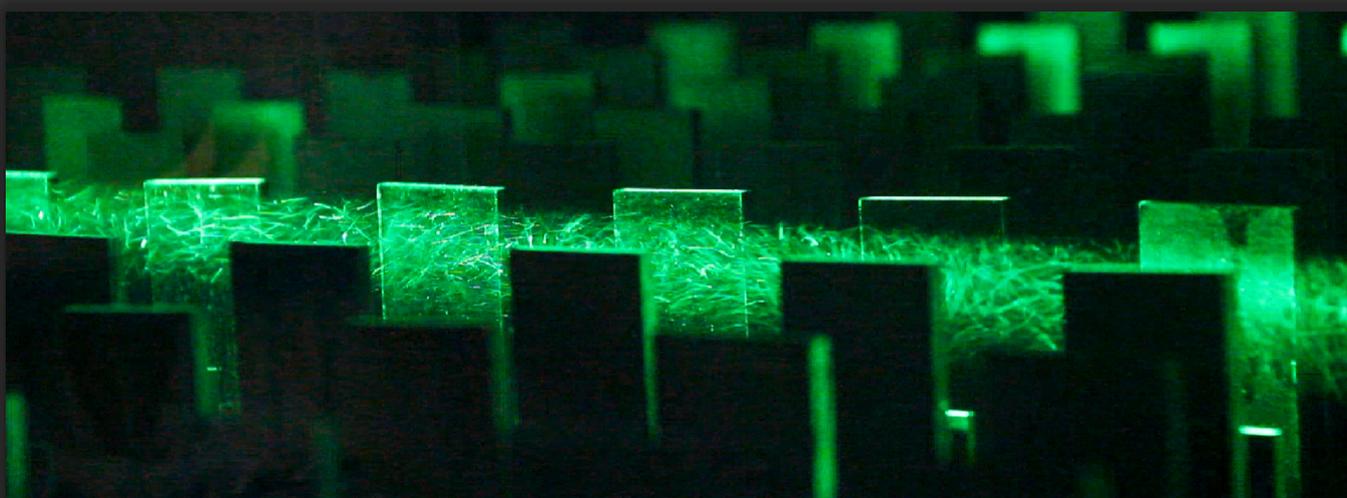


- library, 'liboptv', ANSI C



- PyPTV GUI for *liboptv* in Python
- FlowTracks - trajectories database management (see Meller and Liberzon 2016)
- BlobRecorder - proprietary hardware/customized software (see Shnapp et al. arxiv)

Thank you for your attention



Lagrangian Investigation of Canopy Flow Turbulence - Pair Dispersion

Ron Shnapp¹

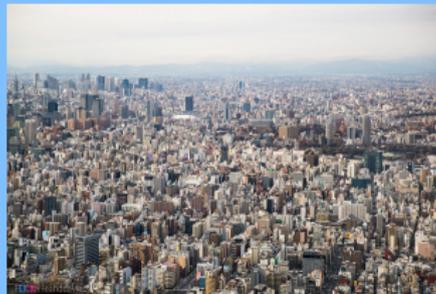
Yardena Bohbot-Raviv², Eyal Fattal², Alex Liberzon¹

¹Tel Aviv University, ²IIBR

Canopy Flows

Flow in the surface layer -

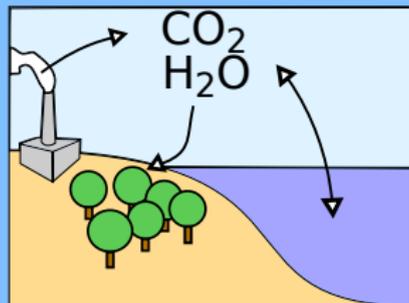
- ▶ Air flow in urban regions
- ▶ Air flow in forests
- ▶ Air flow in fields



Canopy Flows

Determine dispersion, mixing and surface fluxes, e.g. -

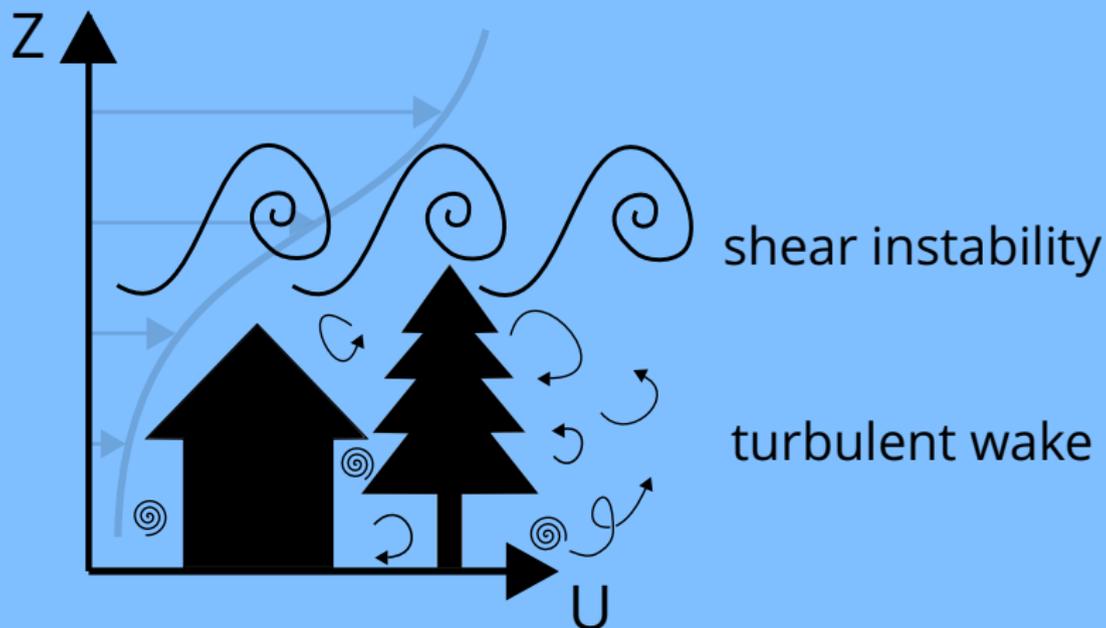
- ▶ Air quality in urban regions
- ▶ H_2O and CO_2 exchange
- ▶ Pollen transport



Images: Carol Clark @ esciencecommons.blogspot,
Seth Anderson @ Flickr

Atmospheric Surface-Layer

- ▶ The bottom part of the ABL
- ▶ **Direct interaction** with the terrain



Very Intense Turbulence!

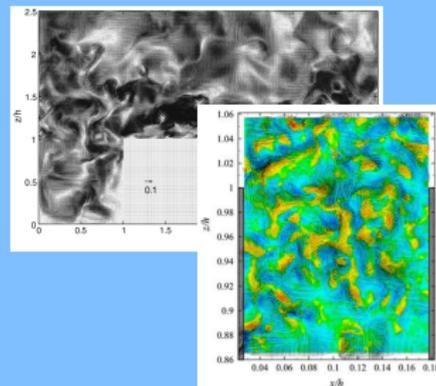
Eulerian Measurements



Stefan Arndt,
University of Melbourne



Kastner-Klein & Rotach (2003)



Coceal et al. (2006)
Zhu, van Hout & Katz (2007)

The *Lagrangian* Description

Specify fluid properties on the positions of fluid tracer particles.



$$\vec{x}(t)$$
$$\vec{v}(t, x(t))$$

Natural in dispersion problems

Lagrangian stochastic models

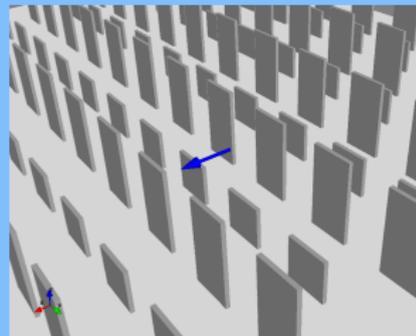
image sources: Seth Anderson @ Flickr

Experimental Data in Canopies is Very Sparse

Methods



Wind Tunnel Model

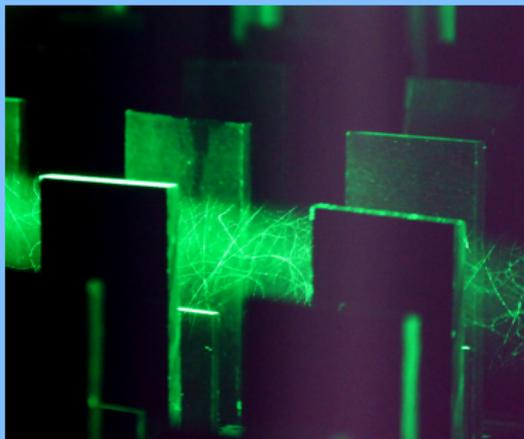
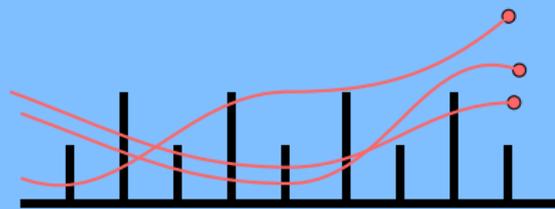


- ▶ IIBR env. wind-tunnel
- ▶ $H = 100$ & 50mm
- ▶ $U_\infty = 2.5$ & 4m/s
- ▶ $Re_\infty = 16$ & 26×10^3

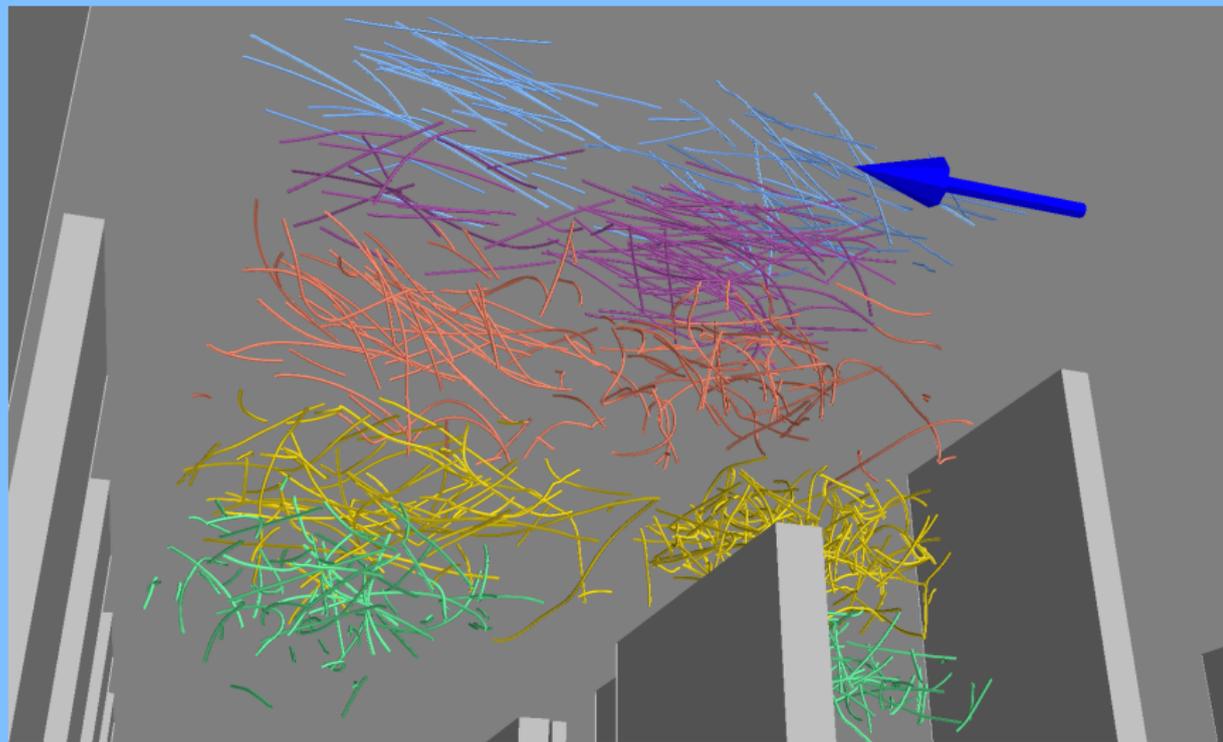
3D-PTV

Lagrangian Data through openPTV -

- ▶ Detection (at 500 & 1000 Hz)
- ▶ Positioning
- ▶ Tracking in 3D



3D-PTV - trajectory dataset

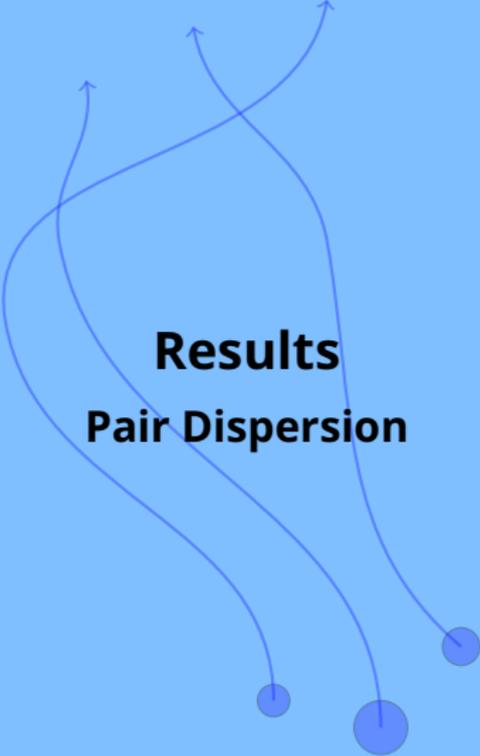


$\sim 6 \times 10^6$ trajectories in and above the canopy layer

3D-PTV - trajectory dataset



go to - <https://youtu.be/NMPCWiWUqrY>

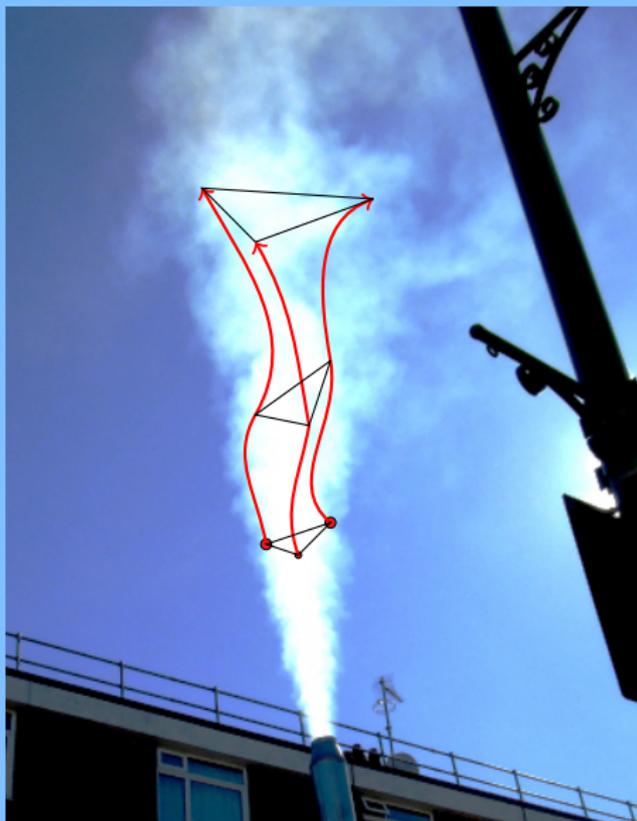
A decorative graphic consisting of three blue circles of varying sizes at the bottom, with three blue lines extending upwards from them. The lines curve and cross each other, ending in arrowheads pointing towards the top of the slide.

Results

Pair Dispersion

Pair Dispersion

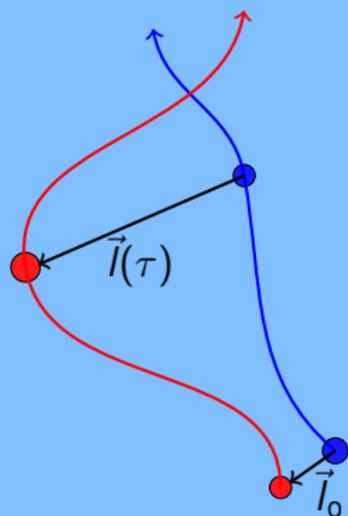
Lagrangian particles as a collective



Pair Dispersion

Consider a **pair** of Lagrangian particles:

- ▶ Distance between the pair $r(t) = |\vec{l}(t)|$
- ▶ The initial separation $r_0 \equiv r(t_0)$
- ▶ The time elapsed $\tau = t - t_0$

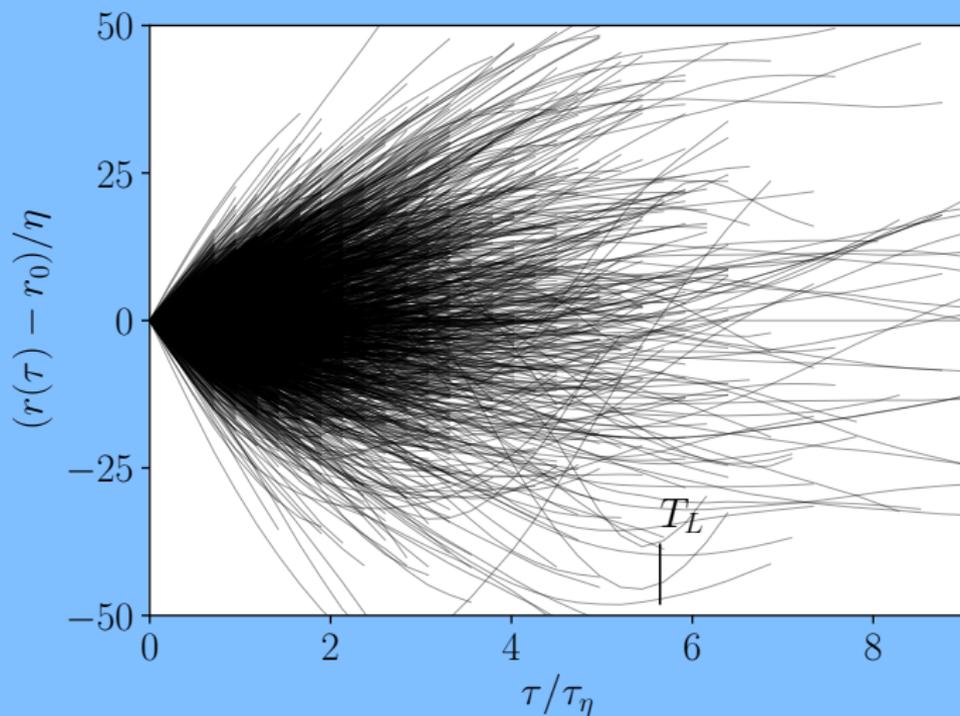


We focus on the change
in separation distance

$$r(\tau) - r_0$$

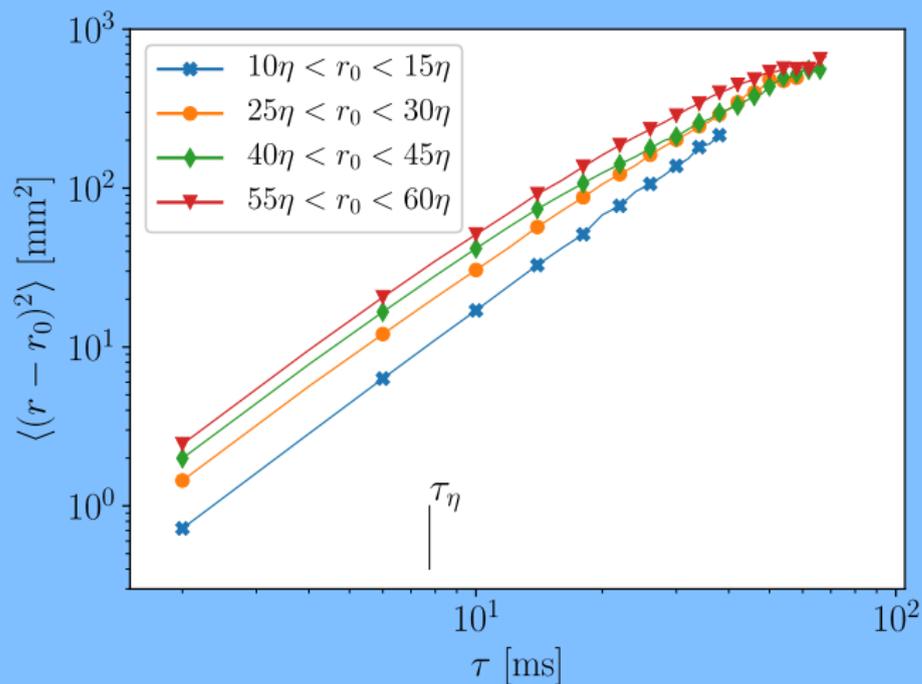
Pair Dispersion

At sub-volume inside the canopy ($\langle z \rangle \approx 0.75H$);
($\sim 0.2 \times 0.5 \times 0.5 H^3$)



Pair Dispersion

Examine the variance as time progresses



dependence on

▶ r_0

▶ τ

Pair Dispersion

Very short times - A Ballistic Regime

$$r(\tau) = r_0 + v_0\tau + \mathcal{O}(\tau^2) \quad \Rightarrow \quad \boxed{\frac{\langle (r - r_0)^2 \rangle}{S_2(r_0) \tau_b^2} = \left(\frac{\tau}{\tau_b} \right)^2}$$

$$\tau_b = \left(\frac{r_0^2}{\epsilon} \right)^{1/3}$$

Here $v_0 \equiv \left. \frac{dr}{d\tau} \right|_0$, $S_2(r_0)$ is the Eulerian second order structure function, and ϵ is the mean rate of dissipation.

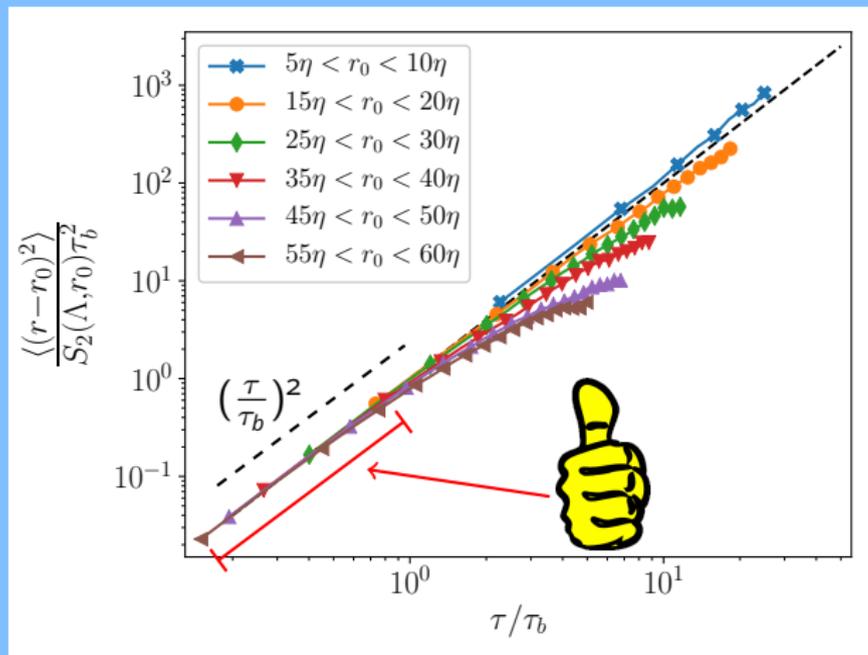
* see the *Ballistic Cascade* phenomenology by Bourgoin (2015).

Pair Dispersion

A Ballistic Regime

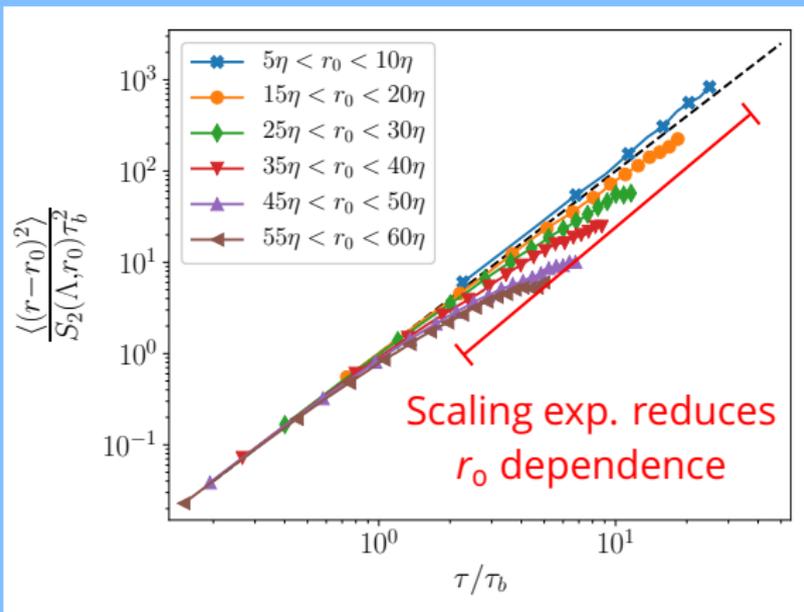
$$\frac{\langle (r - r_0)^2 \rangle}{S_2(r_0) \tau_b^2} = \left(\frac{\tau}{\tau_b} \right)^2$$

Agreement at short times!



Pair Dispersion

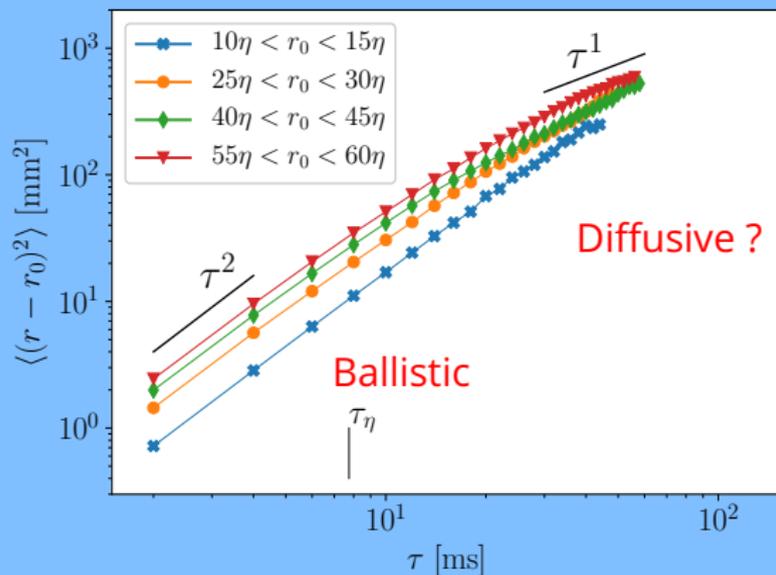
At Longer times



Pairs at different r_0
depart the Ballistic
Regime at different τ_b

Pair Dispersion

At Longer times



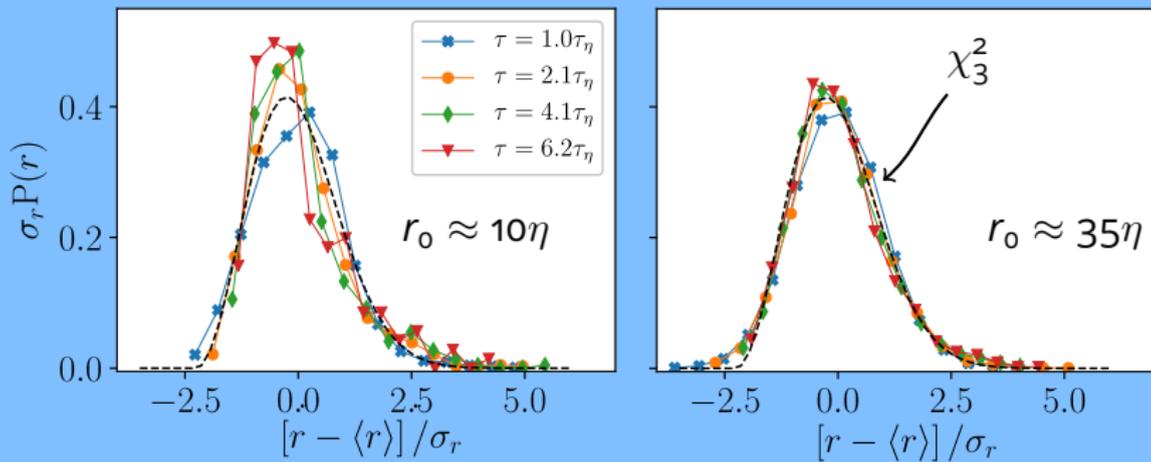
- ▶ Approach to an asymptotic $\propto \tau^1$
- ▶ Diffusive separation?
- ▶ Suggests a decorrelation of particle velocities

Pair Dispersion

At Longer times

If pair velocities are uncorrelated then $l_i = x_i^{(1)} - x_i^{(2)} \sim N(\mu, \sigma)$, and therefore* -

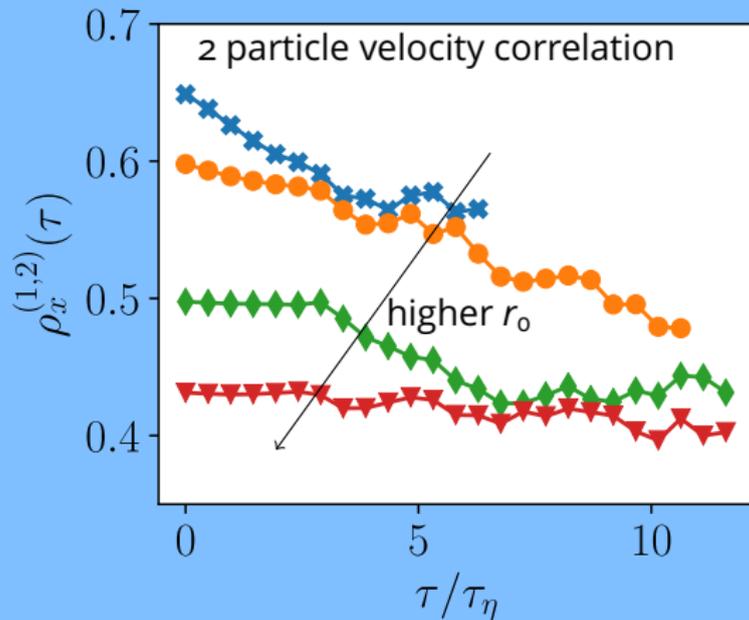
$$r^2 \sim \chi_3^2$$



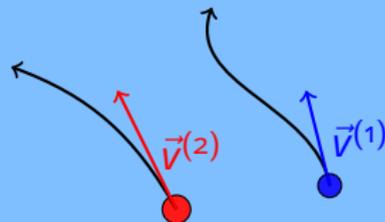
* P. K. Yeung, Physics of Fluids (1994)

Pair Dispersion

At Longer times



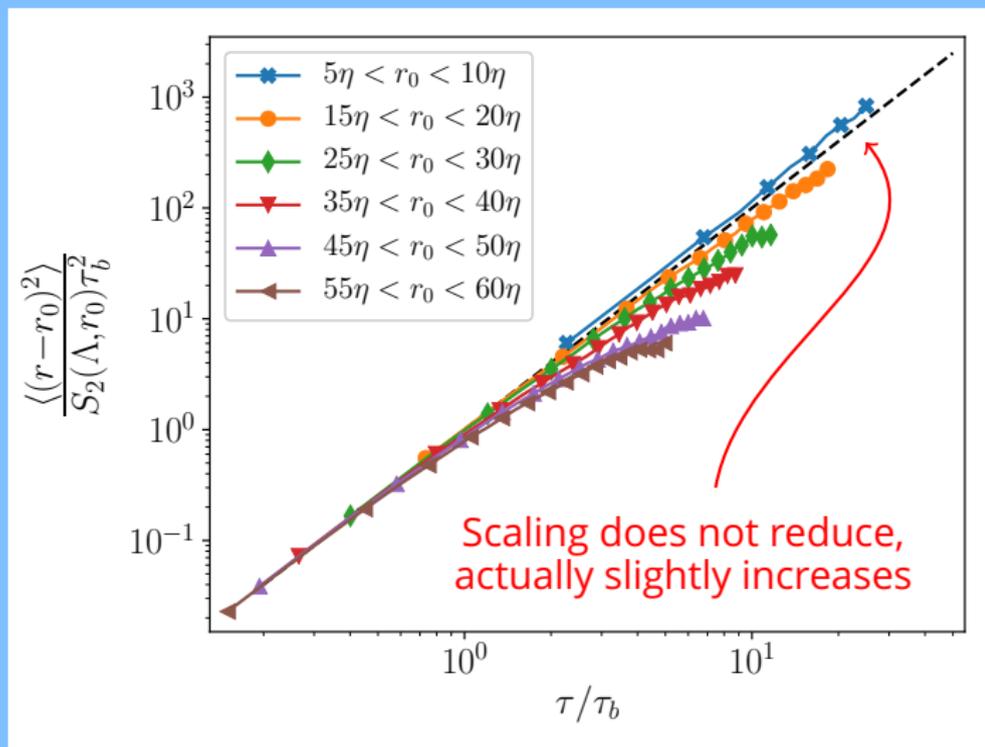
Decorrelation depend on r_0 .



Pairs with **Lagrange** r_0 are **uncorrelated** \Rightarrow Diffusive Separation

Pair Dispersion

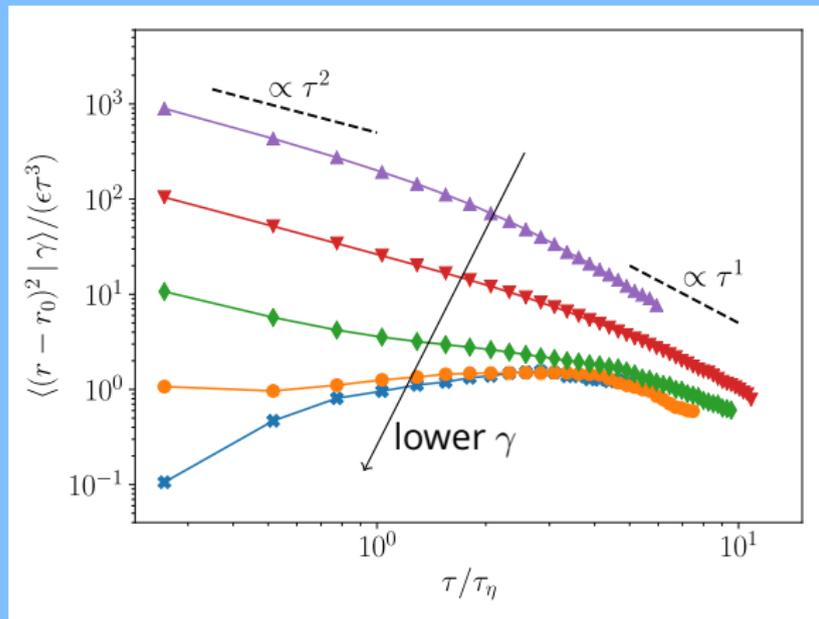
At Longer times & small r_0



Pair Dispersion

At Longer times & small r_0

Instead of r_0 we suggest* $\gamma = \frac{v_0^2}{(\epsilon r_0)^{2/3}}$



For small γ , pairs follow the scaling of the Richardson Obukhov law

$$\langle (r - r_0)^2 \rangle \propto \epsilon \tau^3$$

* Shnapp & Liberzon, PRL (2018)

Conclusions



Conclusions

Pair dispersion:

1. Large r_0 : Ballistic \rightarrow Diffusive
loss of correlation at some length scale
2. Small r_0 : Ballistic \rightarrow Super-Diffusive
ISR scaling + Lagrangian intermittency

I did not discuss: Anisotropy, Inhomogeneity, Large scales

* Shnapp et al. (2019) [arXiv:1806.04975]

* Shnapp and Liberzon; PRL (2018)

Conclusions

I would like to thank

1. The organizers of NCTRV
2. Prof. Alex Liberzon, Dr. Yardena Bohbot-Raviv and Dr. Eyal Fattal
3. Tel Aviv University, school of mechanical engineering
4. PAZY foundation
5. And...

Thank You!